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## Interim Report

IR-13-070

### **Abrupt community transitions and cyclic evolutionary dynamics in complex food webs**

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June 2015

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1           **Abrupt community transitions and cyclic evolutionary dynamics**  
2                           **in complex food webs**

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20  
21   **Abstract**

22   Understanding the emergence and maintenance of biodiversity ranks among the most  
23   fundamental challenges in evolutionary ecology. While processes of community  
24   assembly have frequently been analyzed from an ecological perspective, their  
25   evolutionary dimensions have so far received less attention. To elucidate the  
26   eco-evolutionary processes underlying the long-term build-up and potential collapse of  
27   community diversity, here we develop and examine an individual-based model  
28   describing coevolutionary dynamics driven by trophic interactions and interference  
29   competition, of a pair of quantitative traits determining predator and prey niches. Our

30 results demonstrate the (1) emergence of communities with multiple trophic levels,  
31 shown here for the first time for stochastic models with linear functional responses, and  
32 (2) intermittent and cyclic evolutionary transitions between two alternative community  
33 states. In particular, our results indicate that the interplay of ecological and evolutionary  
34 dynamics often results in extinction cascades that remove the entire trophic level of  
35 consumers from a community. Finally, we show the (3) robustness of our results under  
36 variations of model assumptions, underscoring that processes of consumer collapse and  
37 subsequent rebound could be important elements of understanding biodiversity  
38 dynamics in natural communities.

39

40 **Keywords:** individual-based model; extinction cascade; trophic-level evolution;  
41 consumer collapse

42

## 43 **1 Introduction**

44 Biodiversity emerges over time through speciation and extinction. Species evolve  
45 subject to ecological constraints, which stem from the interactions among them. A  
46 recent study of environmental change and species extinction suggests that the dynamical  
47 change of species interactions is an important proximate cause of species extinction  
48 (Cahill *et al.*, 2012), thus highlighting the importance of understanding the  
49 eco-evolutionary processes and mechanisms that maintain evolved biodiversity.

50 The last few decades have seen impressive advances in our theoretical  
51 understanding of eco-evolutionary dynamics. In community evolution, the main focus is  
52 on understanding the dynamics and complexity of food webs (e.g., Verhoef & Morin,  
53 2010), and much research has been devoted to analyzing models that describe food-web  
54 formation and maintenance (Caldarelli *et al.*, 1998; Drossel *et al.*, 2001, 2004;  
55 Christensen *et al.*, 2002; Yoshida, 2002, 2006; Rosenberg *et al.*, 2005, 2006, 2008;  
56 Stauffer *et al.*, 2005; He & Yu, 2006; Ito & Ikegami, 2006; Bell, 2007; Rikvold, 2007,

57 2009; Rikvold & Sevim, 2007; Guill & Drossel, 2008; Guttenberg & Goldenfield, 2008;  
58 Pękaliski *et al.*, 2008; Ingram *et al.*, 2009; Ito *et al.*, 2009; Powell & Boland, 2009;  
59 Murase *et al.*, 2010; see also the recent review by Brännström *et al.*, 2012). Such  
60 models are typically extended predator–prey models with interactions depending on  
61 assigned traits, so that food webs can ultimately emerge through evolution of these traits.  
62 A surprising finding in many studies is that communities sometimes exhibit a sudden  
63 transition from one evolutionary state to another (Christensen *et al.*, 2002; Ito &  
64 Ikegami, 2006; Rikvold 2007, 2009; Guill & Drossel, 2008; Rossberg *et al.*, 2008;  
65 Murase *et al.*, 2010).

66         Using an individual-based model of evolutionary food-web emergence  
67 without adaptive foraging, Rikvold (2009) found a sudden transition between two  
68 states: a community with multiple trophic levels and a community with only producer  
69 species. Although that study suggested that the emergence of intraspecific predation  
70 could initiate successive consumer extinction in the diverged community, it did not  
71 provide an explanation of the mechanisms that would quickly remove almost all  
72 consumer species from a community. Ito & Ikegami (2006) also found evolutionary  
73 transitions between highly diversified and poorly diversified communities. Other  
74 authors observed fluctuating dynamics of species richness without significant  
75 transitional dynamics (Rossberg *et al.*, 2008; Guill & Drossel, 2008). So far, however,  
76 no mechanistic explanation of the intermittent evolutionary dynamics observed in all  
77 those models has been provided.

78         Most models of community evolution mentioned above focus on speciation–  
79 extinction dynamics by regarding species as the unit of the modeled community and by  
80 considering mutation as being equivalent to speciation (Drossel *et al.*, 2001, 2004;  
81 Christensen *et al.*, 2002; Yoshida, 2002, 2006; Rossberg *et al.*, 2005, 2006, 2008;  
82 Stauffer *et al.*, 2005; He & Yu, 2006; Bell, 2007; Rikvold, 2007; Rikvold & Sevim,  
83 2007; Guill & Drossel, 2008; Guttenberg & Goldenfield, 2008; Pękaliski *et al.*, 2008;

84 Ingram *et al.*, 2009; Powell & Boland, 2009; Murase *et al.*, 2010). However, this  
85 approach to modeling speciation, which forgoes a detailed accounting of the  
86 mechanisms of mutation accumulation and trait divergence, precludes an understanding  
87 of species emergence as an adaptive process.

88 Here, we investigate trophic interactions in a multi-dimensional continuous  
89 niche space through an individual-based stochastic model with the aim of elucidating  
90 the evolutionary processes that lead to the emergence and collapse of multi-layered  
91 communities.

92

## 93 **2 Methods**

94 We consider an individual-based stochastic model in continuous time, in which birth  
95 and death events are realized with probabilistic rates that depend on foraging success,  
96 predation pressure, and interference competition. Selection on foraging and  
97 vulnerability traits, which are inherited nearly faithfully by the asexually produced  
98 offspring, over time leads to the emergence of clusters of related individuals in trait  
99 space, which we identify as species. These species, together with the trophic  
100 interactions among them, define the food web, of which we analyze the structure,  
101 stability, and certain network properties. The details of our model are described below.

102

### 103 **2.1 Evolving traits**

104 Each individual is assumed to be haploid with nearly faithful asexual reproduction. All  
105 individuals are thus considered to reproduce clonally and to produce mutated offspring  
106 with a small probability. Each individual has two sets of quantitative trophic traits:  
107 foraging traits and vulnerability traits. Both sets of traits are represented by  
108 two-dimensional vectors. Following previous work by Ito & Ikegami (2006) and  
109 Rossberg *et al.* (2006), the foraging trait vector of the  $i$ th individual,  $f_i$ , represent its  
110 niche as a consumer, while the vulnerability trait vector  $v_i$  represents its vulnerability

111 to foraging, that is, the niche it provides as a resource. Like these authors, we do not  
112 assign specific biological interpretations (with reference to features such as color or  
113 toxicity) to any axes or points in the trait space; instead, we consider this space as an  
114 abstract representation of all relevant biological traits.

115

## 116 **2.2 Demographic dynamics**

117 We consider birth and death events, which increase and decrease the total population  
118 abundance by 1, respectively. Events are realized sequentially one after the other, and  
119 average waiting times are exponentially distributed, following a Poisson process.

120 We implement the resulting stochastic demographic dynamics using the  
121 Gillespie algorithm (Gillespie, 1976, 1977). Event rates depend on the intensities  $F$   
122 and  $I$  of foraging and interference competition, respectively. We assume that those  
123 interaction intensities between two individuals are given by their traits, in conjunction  
124 with a foraging kernel and an interference competition kernel, which are both assumed  
125 to be Gaussian functions,

$$126 \quad \begin{aligned} F(f_i, v_j) &= \exp(-\|f_i - v_j\|^2 / 2\sigma_F^2) / \sqrt{2\pi}\sigma_F \\ I(f_i, f_j) &= \exp(-\|f_i - f_j\|^2 / 2\sigma_I^2) / \sqrt{2\pi}\sigma_I, \end{aligned} \quad (1)$$

127 with  $\sigma_F$  and  $\sigma_I$  being the standard deviations, or widths, of those kernels.  
128 Interactions become more specific for small widths, and less specific for large widths.  
129 The foraging intensity is higher when a consumer's foraging traits and a resource's  
130 vulnerability traits are more similar, corresponding to an overlap of the utilizable niche  
131 of the consumer and the providing niche of the resource. Moreover, the intensity of  
132 interference competition is maximal between individuals with the same foraging traits,  
133 as consumers can be expected to interfere with one another most strongly when utilizing  
134 the same resource.

135 To prevent runaway selection, we furthermore assume a cost for vulnerability  
136 traits that increases quadratically with their distance from the origin,  $D(v_i) = \|v_i\|^2$ . We

137 assume the availability of an external resource, with vulnerability trait vector  $v_R$  and  
 138 abundance  $N_R$ . For simplicity, we set the vulnerability trait vector of the external  
 139 resource equal to the origin,  $v_R = (0, 0)$ .

140 Based on the assumptions above, the instantaneous rates of birth events,  $r_{bi}$ ,  
 141 and of death events,  $r_{di}$ , of the  $i$ th individual are given by

$$\begin{aligned}
 r_{bi} &= aC_F \sum_j F(f_i, v_j) + aC_F F(f_i, v_R) N_R, \\
 r_{di} &= C_F \sum_j F(f_j, v_i) + C_I \sum_j I(f_i, f_j) + C_D D(v_i) + d.
 \end{aligned}
 \tag{2}$$

143 Here, the summations extend over all individuals in the community, and the coefficients  
 144  $C_F$ ,  $C_I$ , and  $C_D$  scale the intensity of foraging, the intensity of interference  
 145 competition, and the cost of the vulnerability traits, respectively. The remaining  
 146 parameters  $a$  and  $d$  quantify the trophic efficiency and the natural death rate,  
 147 respectively. As event rates are determined by summing over terms that do not depend  
 148 on total population size, the corresponding averaged deterministic dynamics are  
 149 described by multispecies Lotka–Volterra dynamics.

150

### 151 **2.3 Evolutionary dynamics**

152 As we assume haploid individuals with asexual reproduction, mutation is the only  
 153 source of phenotypic variation. We assume a mutation rate proportional to the  
 154 reproduction rate of each individual (Stauffer *et al.*, 2005; He & Yu, 2006; Bell, 2007;  
 155 Rikvold & Sevim, 2007; Rikvold, 2007, 2009; Powell & Boland, 2009; Murase *et al.*,  
 156 2010), with the ratio of those rates being given by a mutation probability. Rossberg *et al.*  
 157 (2006) argued, based on their analysis of empirical data, that the mutation rate of  
 158 foraging traits tends to be much higher than that of vulnerability traits. We therefore  
 159 consider different mutation probabilities for the foraging and vulnerability trait vectors,  
 160  $\mu_f$  and  $\mu_v$ , respectively, with  $\mu_f > \mu_v$ . We assume that the occurrences of mutations  
 161 in foraging and vulnerability traits are independent of each other, so mutations that alter

162 both foraging and vulnerability trait vectors occur with probability  $\mu_f\mu_v$ . A mutation  
163 alters an offspring's trait vector from that of its parent by adding a random vector whose  
164 components are drawn independently from a normal distribution with expectation 0  
165 and variance  $\sigma_m^2$ .

166

## 167 **2.4 Parameter values and initial conditions**

168 Table 1 lists the parameter values we use in our investigations. These are chosen in  
169 agreement with previous theoretical studies, in particular Loeuille & Loreau (2005) and  
170 Rossberg *et al.* (2008). To induce predator–prey diversification, the differentiation  
171 between branched prey species needs to be sufficiently large (Doebeli & Dieckmann,  
172 2000): as the distances among the vulnerability clusters of species are controlled by the  
173 width of the foraging kernel, we assume that the foraging kernel is considerably wider  
174 than the competition kernel.

175 We start our evolutionary investigations with a small population of 100  
176 individuals with foraging and vulnerability traits equal to those of the external resource.  
177 This choice of initial conditions only affects the initial transient dynamics and has no  
178 impact on the long-term outcomes of the investigations.

179

## 180 **2.5 Species determination**

181 Determining what constitutes a species is not trivial when mutational steps are small  
182 and reproduction is asexual. However, in our model, distinct clusters tend to form in  
183 trait space, and the strains in a cluster are mostly close relatives of each other. We can  
184 thus define a species as a cluster of strains in trait space, in accordance with the  
185 genotypic-cluster species concept introduced by Mallet (1995). To identify these  
186 clusters, we apply the QT-clustering algorithm (Heyer *et al.*, 1999) to the distribution of  
187 strains. Due to the small mutation rate, mutation–selection balance can remove all the  
188 relatives of some strains, which results in isolated strains being detected as outliers.



189 Those outlier strains are treated as species consisting of a single trait type.

190

## 191 **2.6 Trophic-level determination**

192 For every species  $i > 0$ , its real-valued fractional trophic level  $t_i$  is calculated  
193 following Odum & Heald (1972) as the weighted average of the trophic level of its prey  
194 species plus 1,

$$195 \quad t_i = 1 + \sum_j w_{ij} t_j. \quad (3)$$

196 Here, the trophic level of the external resource, which can be thought of as the 0th  
197 species, is defined as  $t_0 = 0$ . The weights  $w_{ij}$  are defined by  $w_{ij} = \bar{F}_{ij} / \sum_k \bar{F}_{ik}$  with  
198  $\bar{F}_{ij} = \sum_{x \in S_i} \sum_{y \in S_j} F(f_x, v_y) / n_i$ . Here,  $S_i$  and  $S_j$  are the sets of individuals that  
199 belong to species  $i$  and  $j$ , respectively, and  $n_i$  is the abundance of species  $i$ . The  
200 weight  $w_{ij}$  thus measures the fraction of the average energy input an individual of  
201 species  $i$  receives from all individuals of species  $j$ . Eqs. (3) define a linear system in  
202 which the trophic levels  $t_1, t_2, \dots$  appear as unknowns; this system is solved by  
203 elementary matrix algebra.

204 For  $i > 0$ , the trophic levels thus determined are always larger than or equal  
205 to 1. Species in our model community tend to cluster around integer trophic levels; we  
206 can thus naturally classify species by their trophic level as producers ( $1 \leq t_i < 1.5$ ),  
207 trophic-level-2 consumers ( $1.5 \leq t_i < 2.5$ ), trophic-level-3 consumers ( $2.5 \leq t_i < 3.5$ ),  
208 and so on.

209

## 210 **3 Results**

211 The individual-based stochastic model described above allows for the emergence of  
212 diverse communities with several trophic levels.

213 After an initial transient phase, the abundance of individuals fluctuates over  
214 time, but mostly takes values in two markedly different ranges (Fig. 1), similar to the

215 flip-flop dynamics reported by Rikvold (2009). These ranges correspond to two  
216 characteristic community states. We refer to these community states as the  
217 low-trophic-level (LTL) state and the high-trophic-level (HTL) state. An LTL  
218 community mainly consists of highly abundant producers, while trophic-level-2  
219 consumers are rare and ephemeral (Fig. 1a). In contrast, an HTL community comprises  
220 also higher-trophic-level consumers (Fig. 1b).

221 Evolution is characterized by long periods of HTL and LTL states punctuated  
222 by fast transitions. Below we offer a process-based explanation for the observed  
223 evolutionary dynamics, and also demonstrate that our results remain robust to changes  
224 in parameter values and model assumptions.

225 We now describe these findings in turn. All model parameters used for this  
226 investigation are specified in Table 1 (for the parameters used for the robustness checks,  
227 see Section 3.4).

228

### 229 **3.1 Emergence of complex food webs with multiple trophic levels**

230 Over time, demographic changes and small mutational steps lead to the emergence of a  
231 large number of species organized in several trophic levels. Figure 1 shows the typical  
232 structures of the emerging communities. In the HTL state, communities include  
233 producers and higher-trophic-level species, exhibiting three distinct trophic levels  
234 (Fig. 1b).

235

### 236 **3.2 Community-level evolutionary cycles**

237 Figure 2 shows the total abundance of individuals in the community on a long time  
238 scale. This abundance tends to remain around either of two levels for long periods, each  
239 corresponding to one of the characteristic community states shown in Fig. 1. As the  
240 presence of trophic-level-2 consumers effectively regulates the abundance of the  
241 producers, the HTL producer community tends to have lower total abundance than the

242 LTL producer community. Occasional mutations from producers to trophic-level-2  
243 consumers do occur in the LTL state, but they typically fail to establish.

244           Transitions between these states are relatively fast (Fig. 2a), and we  
245 consistently observe cyclic evolutionary dynamics (Fig. 2b). The distributions of  
246 durations of both LTL and HTL states better match exponential distributions than  
247 power-law distributions (Fig. 2c, d), suggesting that transitions between the two states  
248 are triggered by rare random events that occur with constant probabilities per unit time.

249

### 250 **3.3 Understanding the evolutionary cycles**

251 We now present a detailed analysis of the observed evolutionary cycles (Fig. 2b).  
252 Starting from the LTL state, Figure 3 shows the key steps in a schematic diagram. In  
253 practice, the steps constituting the fast transitions may occur nearly simultaneously.

254           In the LTL state, producers initially mainly diversify in their foraging traits,  
255 so as to avoid interference competition. At the same time, they form relatively large  
256 clouds in terms of their vulnerability traits, because there is little selection pressure on  
257 those. Initially, the number of such clouds almost equals the number of producers  
258 during the preceding HTL state. Gradually, however, the number of those clouds  
259 decreases through random extinctions. Also, the occasional and temporary emergence  
260 of a trophic-level-2 consumer imposes strong foraging pressure on one of those clouds,  
261 and thereby increases its risk of random extinction. Because of those processes, only a  
262 few vulnerability clouds survive the LTL period. While all vulnerability trait vectors  
263 evolve toward the cost minimum at the origin, directional selection ceases at some  
264 distance from the origin, since this allows producers to avoid being foraged by other  
265 producers.

266           The transition from the LTL state to the HTL state is initiated by the  
267 appearance of a mutant individual with foraging traits that allow it to forage on the  
268 extant producer species. This mutant tends to be the offspring of a producer with a

269 foraging trait vector that is already relatively far away from the vulnerability trait vector  
270 of the external resource (i.e., the origin). As only a few vulnerability clouds exist at the  
271 end of the LTL period, the newly emerged consumer species can typically forage on a  
272 large number of producer species, making it a sort of generalist. Consumer control now  
273 regulates producer abundance, leading to increasing producer evenness (Fig. 4a). The  
274 proportion of foraged producers very quickly increases from 0 to 1 (Fig. 4b).  
275 Because of the foraging pressure, the abundances of the producers quickly decrease,  
276 leading to the eventual (stochastic) extinction of a number of producers due to  
277 overexploitation, in what can be viewed as a top-down process.

278         The extinction of some producers leads to mounting foraging pressure by the  
279 generalist consumer on the remaining producers, generating a strong selection pressure  
280 towards a diversification of their vulnerability traits. This promotes differentiation of  
281 the vulnerability trait vectors within the producer community. The foraging traits of the  
282 trophic-level-2 consumer undergo a corresponding specialization, resulting in the  
283 emergence of trophic-level-2 consumers each specialized on one producer species.  
284 Because we assume that the costs associated with vulnerability trait vectors increase  
285 with their distance from the origin, the process of diversification ceases once the viable  
286 vulnerability trait space is mostly occupied by producers. This is the HTL community  
287 state. The HTL producers are diversified in their foraging trait vectors (because of  
288 interference competition) as well as in their vulnerability trait vectors (because of  
289 foraging pressure). The trophic-level-2 consumers of the HTL state are diversified in  
290 their foraging trait vectors, but not so much in their vulnerability trait vectors (for the  
291 same reason that LTL producers are not, i.e., because of the absence of predation). The  
292 high evenness among producers suggests that producer abundances are strongly  
293 controlled by consumers (Fig. 4a,c). A generalist trophic-level-3 consumer foraging on  
294 trophic-level-2 consumers can also emerge. More complex communities rarely evolve  
295 in our model, except for extreme parameter settings ( $a = 0.9$ , Fig. S2), because the

296 strongly decreasing abundance of the higher-trophic-level species makes their  
297 persistence less likely.

298           The random extinction of a trophic-level-2 consumer initiates the transition  
299 from the HTL state to the LTL state. Since producers are mostly foraged on by  
300 specialists, the extinction of such a specialist consumer removes the foraging pressure  
301 from the corresponding producer. As a consequence, the abundance of this producer  
302 quickly increases, which, in turn, increases the level of interference competition exerted  
303 by it. Strong interference competition effectively decreases the abundance of the other  
304 producers, and consequently, the abundance of the corresponding trophic-level-2  
305 consumers, threatening their survival (and the survival of all higher-trophic-level  
306 consumers). This destabilization of the producer level manifests itself in terms of  
307 decreasing producer evenness, which slightly precedes the decrease in consumer  
308 richness (Fig. 4c). As more and more higher-trophic-level species become extinct, the  
309 proportion of producers that are free from foraging pressure increases (Fig. 4d), and so  
310 does the competitive pressure on the remaining pairs of producers and trophic-level-2  
311 consumers. Ultimately, only a few producer species survive, which means that the  
312 community has reverted to its initial state. This extinction of the higher-trophic-level  
313 species can be seen as a bottom-up extinction process, as it is driven by the competitive  
314 dynamics of producer species.

315

### 316 **3.4 Robustness of the evolutionary cycles**

317 To explore the robustness of our results, we consider alternative minima of the  
318 vulnerability costs, different dimensionalities of the trophic trait space, variation in four  
319 salient model parameters, and nonlinear functional responses.

320           First, we relax the assumption that the cost minimum for vulnerability traits  
321 coincides with the vulnerability trait of the external resource (Fig. S1). We find that the  
322 re-emergence of the trophic structure becomes difficult when this difference is made

323 large, but at the same time we can confirm that the results presented here remain valid  
324 for small to moderate differences.

325         Second, we investigate the effect of altering the trait-space dimensionality on  
326 the cyclic evolutionary dynamics (Fig. S2). We relax the assumption that vulnerability  
327 trait vectors and foraging trait vectors are two-dimensional and investigate also one-,  
328 three-, and four-dimensional trait vectors. In a few selected trials (limited by the rapidly  
329 increasing computational time), we find qualitatively similar outcomes – cyclic  
330 transitions between HTL states and LTL states – with the relative duration of the LTL  
331 state increasing with the dimensionality.

332         Third, we increase the trophic efficiency  $a$  from 0.2 to 0.9, which results  
333 in qualitatively similar intermittent dynamics, except that for higher trophic efficiencies  
334 food webs with higher abundances, larger species richness, and higher trophic levels  
335 evolve (Fig. S3). Larger trophic efficiencies directly increase the energy flow from the  
336 external resource to consumers, and therefore can maintain a larger number of  
337 consumers, enabling the evolution of higher-trophic-level species. In turn, larger  
338 consumer abundances decrease demographic stochasticity, and thus increase the relative  
339 duration of the HTL state. Nevertheless, the HTL-to-LTL transition is eventually still  
340 triggered by the extinction of a trophic-level-2 consumer.

341         Fourth, we increase the abundance  $N_R$  of the external resource by a factor of  
342 2 (from  $N_R = 4,500$  to 9,000), which raises the observed total abundance as well as  
343 the abundance within all species by roughly the same factor (Fig. S4). We find that the  
344 community's overall behavior remains very similar, except for a prolonged duration of  
345 the HTL state due to diminished demographic stochasticity.

346         Fifth, varying the scales of foraging intensity and interference-competition  
347 intensity ( $C_F = 0.45, 0.9, \text{ or } 1.8$ ;  $C_I = 0.05, 0.1, \text{ or } 0.2$ ) results in one of three  
348 patterns: (1) a stable LTL community, (2) evolutionary cycling, or (3) complete  
349 extinction (Figs. S5). A larger foraging intensity improves the effectiveness of resource

350 consumption, which enables a consumer to survive with fewer resources. It thus  
351 facilitates the establishment of consumers, which marks the beginning of the  
352 evolutionary cycle. Overexploitation, in contrast, leads to extinction.

353 Sixth, we relax the assumption that the offspring trait distributions have the  
354 same variances for foraging and vulnerability traits (Fig. S6). Introducing separate  
355 variances for foraging and vulnerability traits,  $\sigma_{m,f}^2$  and  $\sigma_{m,v}^2$ , respectively, by fixing  
356  $\sigma_{m,v} = 0.03$  and varying  $\sigma_{m,f}$  to equal 0.01 or 0.09, we find that a smaller  $\sigma_{m,f}^2$   
357 causes the abundance in the LTL state to become higher and consumers to die out. With  
358 a larger  $\sigma_{m,f}^2$ , on the other hand, the HTL state is stabilized, and the recovery time from  
359 the LTL state to the HTL state is shortened. This is as expected: in the latter case,  
360 consumers can switch their resource more easily, keeping the producers under consumer  
361 control and thus preventing the community's collapse, while in the former case,  
362 producers can more easily evolve away from their consumers, freeing them from  
363 consumer control and thus triggering the community's collapse. While the waiting time  
364 until community collapse is thus changing, the overall community dynamics remain  
365 largely the same.

366 Seventh and finally, we introduce handling times, by considering a  
367 Holling-type-II functional response instead of a linear functional response (Fig. S7). If  
368 the handling times are sufficiently small, we observe the same evolutionary cycles as  
369 with the linear response; otherwise, the evolved consumer species tend to become  
370 extinct quickly, and the HTL state is not established.

371

## 372 **4 Discussion**

373 In this study, we have introduced and investigated a stochastic individual-based model  
374 of coevolutionary dynamics driven by predation and interference competition.  
375 Individuals are fully described by vulnerability and foraging trait vectors, characterizing  
376 their ecological niche. Over time, demographic dynamics with small mutations in these

377 traits lead to the establishment of large interconnected ecological communities with  
378 three to four trophic levels. The subsequent evolutionary dynamics are characterized by  
379 relatively long periods that the community spends around either of two characteristic  
380 states, occasionally punctuated by fast transitions during which the composition of the  
381 community is altered by mass extinctions and rapid diversification, respectively.

382         To the extent that similar transitions happen in natural communities, they  
383 might be triggered more or less easily than in our model. Because of constraints on  
384 computational time, our model community comprises a relatively small number of  
385 individuals as compared with most real ecological communities. This small community  
386 size potentially increases the importance of demographic stochasticity in community  
387 dynamics, in particular for species at higher trophic levels. This demographic  
388 stochasticity might facilitate the triggering of community-level transitions. On the other  
389 hand, in natural communities these transitions might alternatively be triggered by  
390 environmental stochasticity or random external impacts, such as the occasional release  
391 from a natural enemy (Keane & Crawley, 2002); such external drivers are not included  
392 in our model. At any rate, once events have been set in motion towards a transition, the  
393 resultant cascade of coevolutionary changes might well be a community's principal  
394 cause of extinctions.

395         A key element in any model of food-web evolution are the trait values that  
396 characterize an individual. Loeuille & Loreau (2005) and Brännström *et al.* (2011) used  
397 the maximum body size of species as the evolving trait. Guill & Drossel (2008) and  
398 Ingram *et al.* (2009) considered an abstract one-dimensional niche space. In the  
399 Webworld model (Caldarelli *et al.*, 1998; Drossel *et al.*, 2001, 2004) and the  
400 Tangled-Nature model (Christensen *et al.*, 2002; Rikvold, 2007, 2009; Rikvold &  
401 Sevim, 2007), many traits determine both foraging ability and vulnerability, and the  
402 acquisition or loss of such traits are considered as evolutionary steps. Our model is  
403 grounded in a different school of thought, which has traditionally emphasized abstract



404 vulnerability and foraging traits (Rossberg *et al.* 2006, 2010; see also Rossberg *et al.*  
405 2008, which partly bridges between these two schools). In an effort to better understand  
406 the structure of food webs, Rohr *et al.* (2010) carried out a statistical analysis of twelve  
407 empirically documented food webs and found that body size only partially captures the  
408 trophic information embodied in a food web, while the inclusion of latent traits  
409 representing foraging and vulnerability drastically improved statistical fits. In good  
410 alignment with the conclusions of our study, they found that basal species mainly  
411 diversify their vulnerability traits, whereas top predators mainly diversify their foraging  
412 traits. These results support the findings presented here and underscore the importance  
413 of considering both foraging traits and vulnerability traits.

414         Using a ratio-dependent functional response, the Tangled-Nature model may  
415 also exhibit flip-flop dynamics between species-rich communities and  
416 producer-dominated communities (Rikvold, 2009). Based on the analysis of a simplified  
417 two-species model, Rikvold (2009) proposed that the emergence of intra-guild predation  
418 (IGP, i.e., the ability of species to forage on competitors on their own trophic level)  
419 destabilizes a diverse community. In the present study, we have elucidated the detailed  
420 eco-evolutionary mechanisms underlying the entire cyclic dynamics, including the  
421 transitional processes, using a full model featuring an emerging number of species. Our  
422 results suggest that IGP is not a major factor for explaining successive extinctions. If  
423 IGP were a major factor, transitions should be much slower than observed by Rikvold  
424 (2009) and in our model. Furthermore, non-specialist consumers are very rare in the  
425 high-trophic-level (HTL) community state, since the distances among the producer  
426 vulnerability clouds are relatively large. Although Rikvold (2009) did not explicitly  
427 include interspecific competition, a ratio-dependent functional response implicitly  
428 introduces competition between species that share the same resource (Getz, 1984). The  
429 competition-based explanation of cyclic community dynamics we propose here  
430 therefore could also be applied to explaining the flip-flop dynamics observed by

431 Rikvold (2009).

432           It is instructive to compare the cyclic community dynamics of consumer  
433 emergence and collapse reported here to the classical phenomenon of predator–prey  
434 cycling. From this perspective, a community that mainly consists of producers, being in  
435 the low-trophic-level (LTL) community state, is analogous to a prey-abundant  
436 community. When a predator–prey system is in this state, the predator can establish  
437 itself and easily increase its abundance, resulting in the build-up of predation pressure.  
438 This leads to a community in which predator and prey temporarily coexist at relatively  
439 high abundance, analogous to the high-trophic-level (HTL) state of our model, which  
440 also comprises higher-trophic-level consumers. In a predator–prey system, this  
441 gradually engenders a shortage of prey, causing in turn a reduction of the predator  
442 population. Similarly, in our model consumer species start to go extinct once they have  
443 reached a high diversity, owing to foraging-induced extinctions of their resource  
444 species.

445           While these considerations help to appreciate some key similarities between  
446 the predator–prey cycling of population-level demographic states and the cycling of  
447 community-level evolutionary states reported here, an obvious limitation of this analogy  
448 is the relatively short duration of the producer- and consumer-abundant communities in  
449 predator–prey cycling, which contrast with the relatively long durations of the LTL and  
450 HTL states we have observed. The main reason for this difference is that our model  
451 describes not only the demography of trophic interactions but also their evolution and  
452 diversification. The latter being slow processes results in the long durations of the LTL  
453 and HTL states.

454           A key finding of the present study is that the HTL state is unstable: in this  
455 state, a small perturbation is eventually responsible for inducing its collapse. This kind  
456 of instability is by no means coincidental – instead, natural selection at the species level  
457 systematically favors the evolution of such an unstable condition at the community level.

458 A similarly counterintuitive outcome of evolution, evolution toward extinction, is  
459 known as evolutionary suicide, and has been observed in several model systems  
460 (Dieckmann *et al.*, 1995; Ferrière, 2000; reviewed by Parvinen 2005). Likewise, Rand  
461 *et al.* (1995) demonstrated that unstable interspecific interactions can emerge through  
462 the coevolution of host–pathogen interactions. Specifically, they found that, under  
463 certain conditions, the pathogen’s transmissibility evolves to a critical level at which the  
464 host–pathogen system could become extinct. Evolution towards unstable community  
465 states, as observed in the model of Rand *et al.* (1995) and in our model, highlights the  
466 potential for community crashes to occur as the outcome of the evolutionary dynamics  
467 of interspecific interactions.

468         Altering several parameters in our model results in communities that differ in  
469 terms of their species richness, total abundance, and maximum trophic level. Yet, as we  
470 have shown, intermittent and cyclic transitions between HTL and LTL states are  
471 observed for a wide range of model parameters. While this inspires confidence in our  
472 results, an important challenge for future research is to infer reasonable parameter  
473 ranges from empirical data. The most immediate concern might be to improve empirical  
474 estimates of the intensities of foraging and interference competition, as these two  
475 parameters have a particularly strong effect on the presence or absence of cyclic  
476 transitions.

477         As we increase the number of trait-space dimensions, we observe decreasing  
478 durations of the HTL period. This can be explained by the fact that, in  
479 higher-dimensional trait spaces, specialist consumers increasingly tend to “lose” the  
480 producers on which they forage, which results in the emergence of consumer-free  
481 producers and triggers the transition to the LTL state with increasing frequency. For  
482 host–parasite systems, such evasive evolution has been theoretically analyzed by  
483 Gilman *et al.* (2012).

484         Although we observe large intermittent evolutionary avalanches, i.e.,

485 successive speciation and extinction at transitions, we do not find other signatures of  
486 self-organized criticality as defined by Bak *et al.* (1988, 1989), which has been used to  
487 explain the large fluctuations observed in evolutionary food-web models (Rossberg  
488 *et al.*, 2006, 2008; Guill & Drossel, 2008; Rikvold, 2009). Since both HTL and LTL  
489 states have a characteristic species richness, the stochastic transitions between HTL and  
490 LTL states result in the stochastic occurrence of fixed-sized extinction and speciation  
491 cascades, which does not agree with the  $1/f$  noise expected by Bak *et al.* (1988) and  
492 Bak & Sneppen (1993). However, the fact remains that the HTL structure investigated  
493 in this study, into which the system evolutionarily organizes itself so predictably,  
494 represents a fragile community state that, equally predictably, will be destabilized by  
495 eventual random abundance fluctuations.

496 Evolutionarily emerging food webs can be seen as examples of adaptive  
497 networks. Another example are gene-regulatory networks, in which the evolutionary  
498 need to balance phenotype conservation and phenotype innovation leads to critical  
499 dynamics, so that perturbations of gene expression neither amplify nor die out  
500 (Torres-Sosa *et al.*, 2012). We can similarly explain the intermittent dynamics observed  
501 in our model by a sort of conservation–innovation balance, if we liken consumers  
502 remaining specialized on their resource (caused by small mutational variance in  
503 foraging traits) to phenotype conservation, and evolutionary resource switching  
504 (enabled by large mutational variance in foraging traits) to phenotype innovation.  
505 Conservative evolution in this sense tends to the LTL state, while innovative evolution  
506 favors the HTL state; the fact that the community cyclically switches from one state to  
507 the other can be interpreted as an evolutionary attempt to balance conservation and  
508 innovation. This analogy should be taken with a grain of salt, however, since the  
509 underlying model details are rather different. In particular, the selection scheme of  
510 gene-regulatory networks, i.e., selection on the entire network structure and dynamics,  
511 is different from that in food webs, in which selection acts at the individual level, and

512 thus, separately impacts each network node.

513           Our current model assumes a well-mixed community and does not incorporate  
514 extinction–invasion dynamics. On the population-dynamical time scale, local  
515 extinctions and invasions can alter the set of coexisting species (Leibold *et al.*, 2004).  
516 Migration to and from neighboring communities can lead to the extinction of consumer  
517 species, before an abundance explosion of prey species induces secondary extinctions,  
518 and the trophic structure of the whole metacommunity is stabilized. Understanding the  
519 effects of occasional invasions from other ecological communities is important and  
520 would be a worthwhile extension of the work presented here.

521           In this study, we have demonstrated the evolutionary emergence and  
522 breakdown of complex food webs through the coevolution of generic foraging and  
523 vulnerability traits. We hope that the work presented here will contribute to a better  
524 understanding of our rich evolutionary past, and thereby enable an enhanced  
525 appreciation for the eco-evolutionary dynamics that shape our future.

526

## 527 **Acknowledgements**

528 We thank Michio Kondoh, Maurice Sabelis, Arndt Telschow, Shigeo Yachi, Norio  
529 Yamamura, and Katsuhiko Yoshida for discussions, insightful comments, and  
530 suggestions. This research was supported by the Global Center of Excellence Program  
531 A06 at Kyoto University, by the Japan Society for the Promotion of Science (JSPS)  
532 Core-to-Core Program (20004), and by KAKENHI (11007744) from JSPS to A.Y. D.T.  
533 gratefully acknowledges financial support by a JSPS Research Fellowship for Young  
534 Scientists. U.D. gratefully acknowledges financial support by the European Science  
535 Foundation, the Austrian Science Fund, the Austrian Ministry of Science and Research,  
536 and the Vienna Science and Technology Fund, as well as by the European Commission,  
537 through the Marie Curie Research Training Network FishACE and the Specific  
538 Targeted Research Project FinE.

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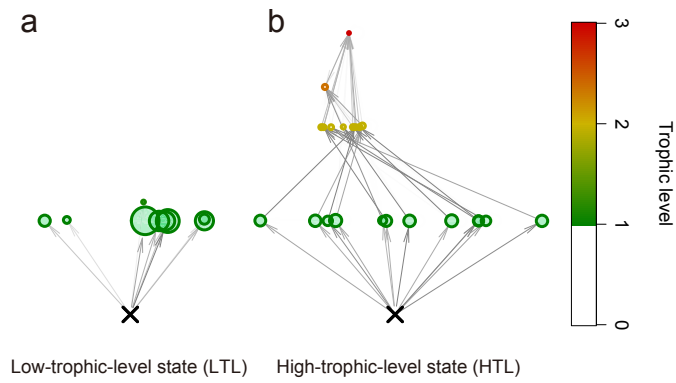
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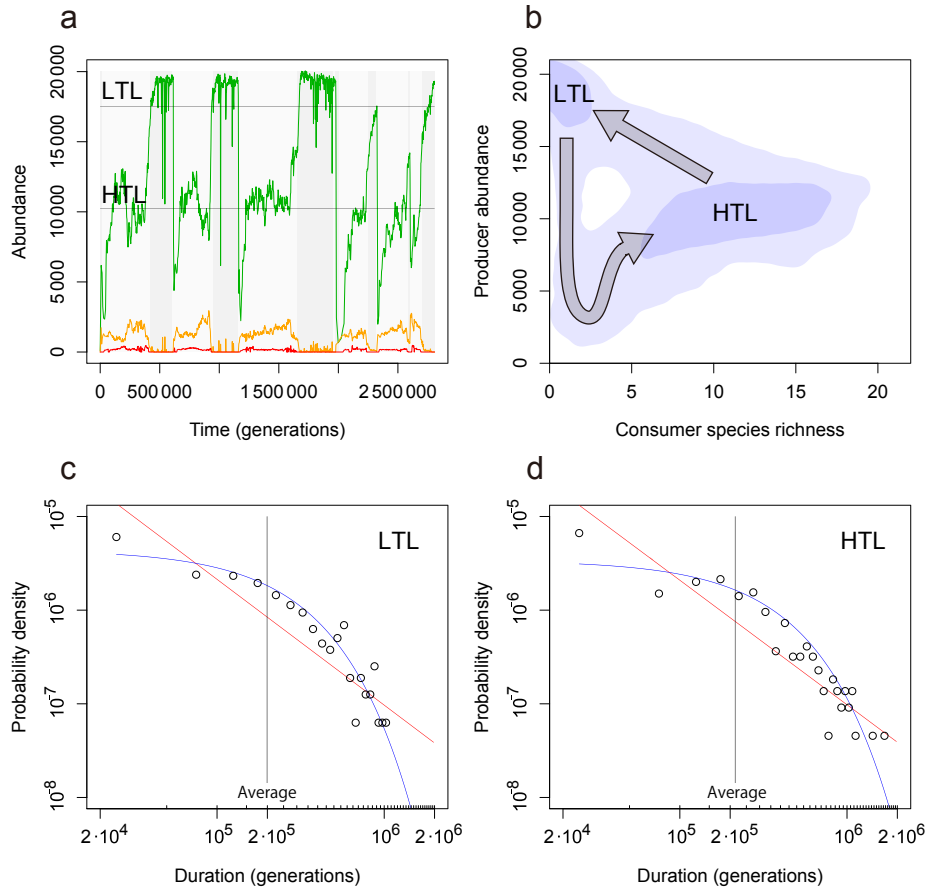
662 **Figures**

663



664 **Figure 1:** Examples of the two distinct community states observed in this study. Each  
665 circle represents a species, with their areas being proportional to the species' abundance,  
666 their colors indicating the species' trophic level, and their horizontal positions  
667 indicating the species' first vulnerability trait. The cross at trophic level 0 represents  
668 the external resource. Arrows indicate trophic links, with darker shades indicating  
669 stronger interactions.

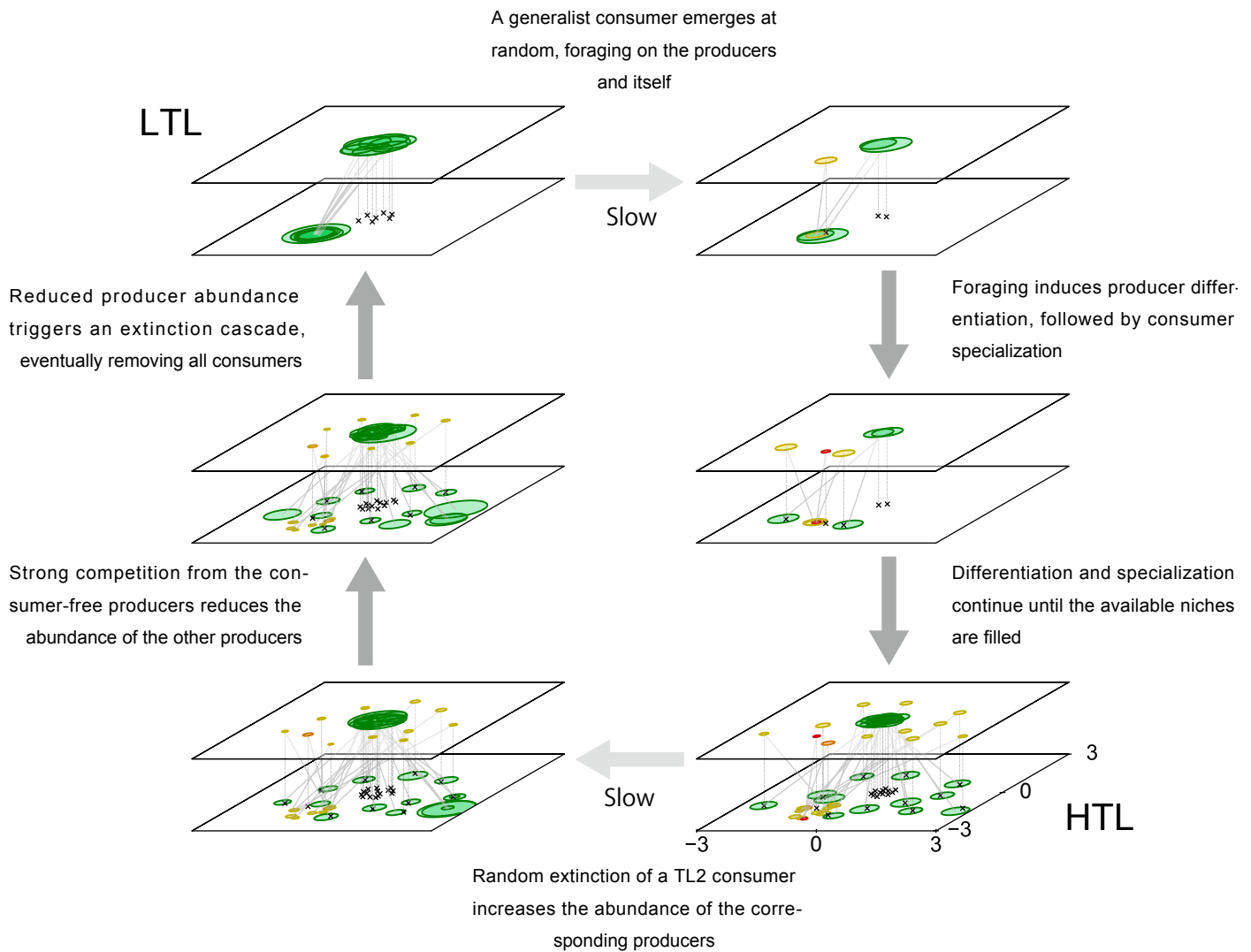
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671

672 **Figure 2:** Cyclic evolutionary transitions between the two community states. (a)  
 673 Continuous curves represent the total abundance of producers (green), trophic-level-2  
 674 consumers (orange), and trophic-level-3 consumers (red). (b) Frequency distribution of  
 675 community states: 99% of community states are observed in the shaded areas, and 75%  
 676 of community states are observed in the dark-shaded areas. (c, d) Probability  
 677 distributions of community-state durations (c: low-trophic-level communities, LTL; d:  
 678 high-trophic-level communities, HTL). Minor ticks indicate the bins used for  
 679 constructing the histogram, red and blue curves indicate the best-fit power-law  
 680 distributions and the best-fit exponential distributions, respectively. The frequency  
 681 distributions shown in (b–d) are obtained by convolving a Gaussian distribution with  
 682 72,060 sampled community states from 60 independent model runs.

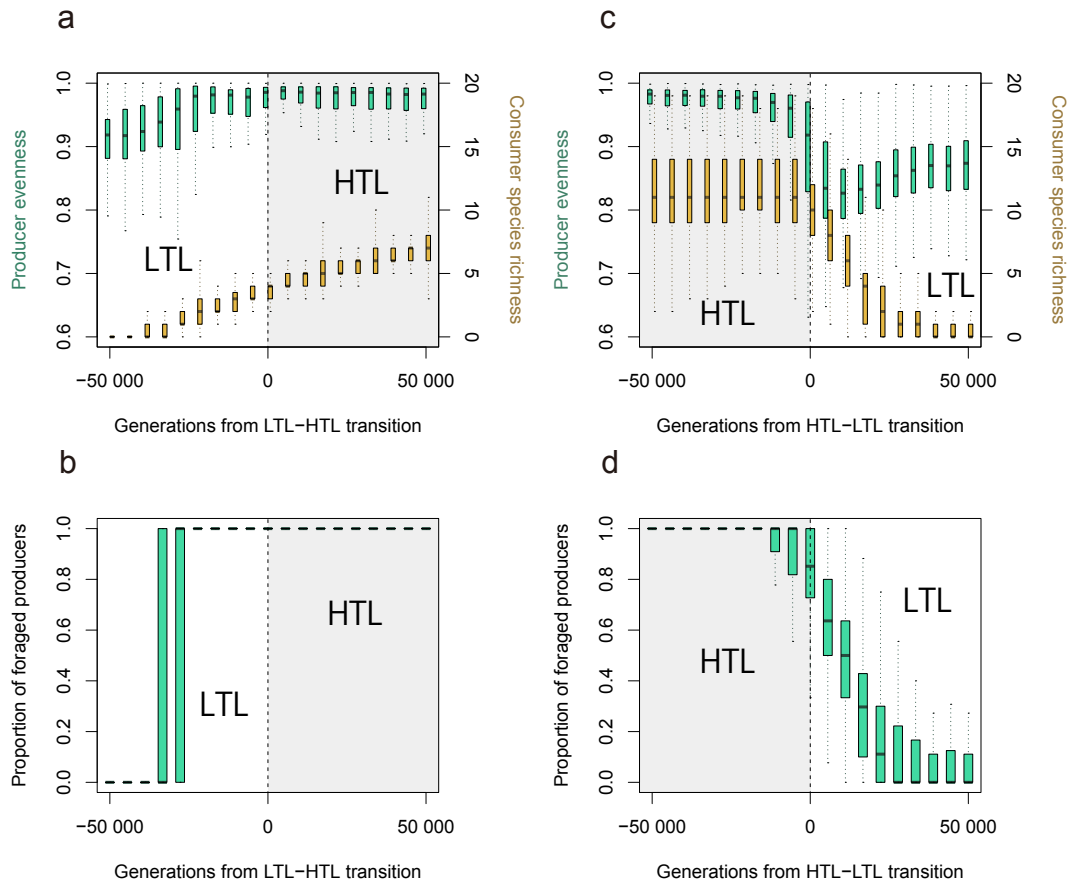
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684

685 **Figure 3:** Mechanistic explanation of the cyclic evolutionary transitions between the  
 686 low-trophic-level (LTL) state and the high-trophic-level (HTL) state. In each panel, the  
 687 top and bottom layers represent the trait spaces of foraging traits and vulnerability traits,  
 688 respectively. The foraging traits and vulnerability traits of a species are indicated by two  
 689 circles, one on the top layer and one on the bottom layer, connected by a gray line. The  
 690 area and color of each such circle indicates a species' abundance and trophic level,  
 691 respectively, as in Fig. 1. For ease of readability, vertical line segments with crosses at  
 692 their lower ends indicate the mean foraging traits of each species, describing where the  
 693 considered species forages most effectively. Dark arrows between the panels indicate

694 fast and potentially concurrent transitions, while light arrows indicate slow transitions  
695 triggered by rare random events.  
696



697 **Figure 4:** Transient dynamics associated with the cyclic evolutionary transitions  
698 between the two community states. Panels (a, b) show the time course during consumer  
699 emergence, while panels (c, d) show the time course during consumer collapse. Shaded  
700 areas highlight the HTL state. (a, c) Green and yellow boxes indicate producer evenness  
701 (Pielou, 1966) and consumer species richness, respectively. (b, d) Green boxes indicate  
702 the proportion of producer species foraged by trophic-level-2 consumers. An  
703 interaction is counted as foraging only if the corresponding trophic link satisfies  
704  $F(f_i, v_j) > 0.5$ . The HTL state is defined as a continuous time interval during which a  
705 community comprises trophic-level-3 -or-higher species. To reduce stochastic  
706 fluctuations, time courses from 60 independent model runs, each comprising more  
707 than 2,000,000 generations, are smoothed by convolution with a Gaussian kernel  
708 prior to the detection of the HTL intervals.  
709

710

Description	Symbol	Value
Abundance of external resource	$N_R$	4,500
Scale of the intensity of foraging	$C_F$	0.9
Scale of the intensity of interference competition	$C_I$	0.1
Scale of the vulnerability costs	$C_D$	20
Trophic efficiency	$a$	0.2
Intrinsic death rate	$d$	0.1
Width of foraging kernel	$\sigma_F$	0.3
Width of competition kernel	$\sigma_I$	0.1
Vulnerability traits of external resource	$v_R$	(0, 0)
Mutation probability of foraging traits	$\mu_f$	0.001
Mutation probability of vulnerability traits	$\mu_v$	0.0001
Width of mutation kernel	$\sigma_m$	0.03

711

712 **Table 1:** Model parameters. The abundance of external resource,  $N_R$ , the scale of the  
713 vulnerability costs,  $C_D$ , and the intrinsic death rate  $d$  can be considered as scaling the  
714 units of population abundance, trait-space distances, and time, respectively.



## Supplemental information:

### Abrupt community transitions and cyclic evolutionary dynamics in complex food webs

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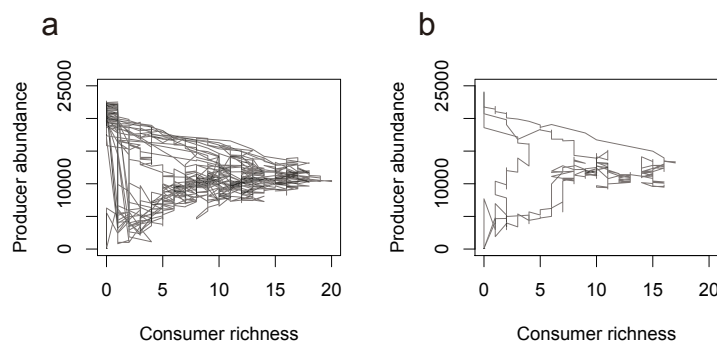
<sup>b</sup> Department of Mathematics and Mathematical Statistics, Umeå University, 901 87 Umeå, Sweden

<sup>c</sup> Evolution and Ecology Program, International Institute for Applied Systems Analysis (IIASA), Schlossplatz 1, 2361 Laxenburg, Austria

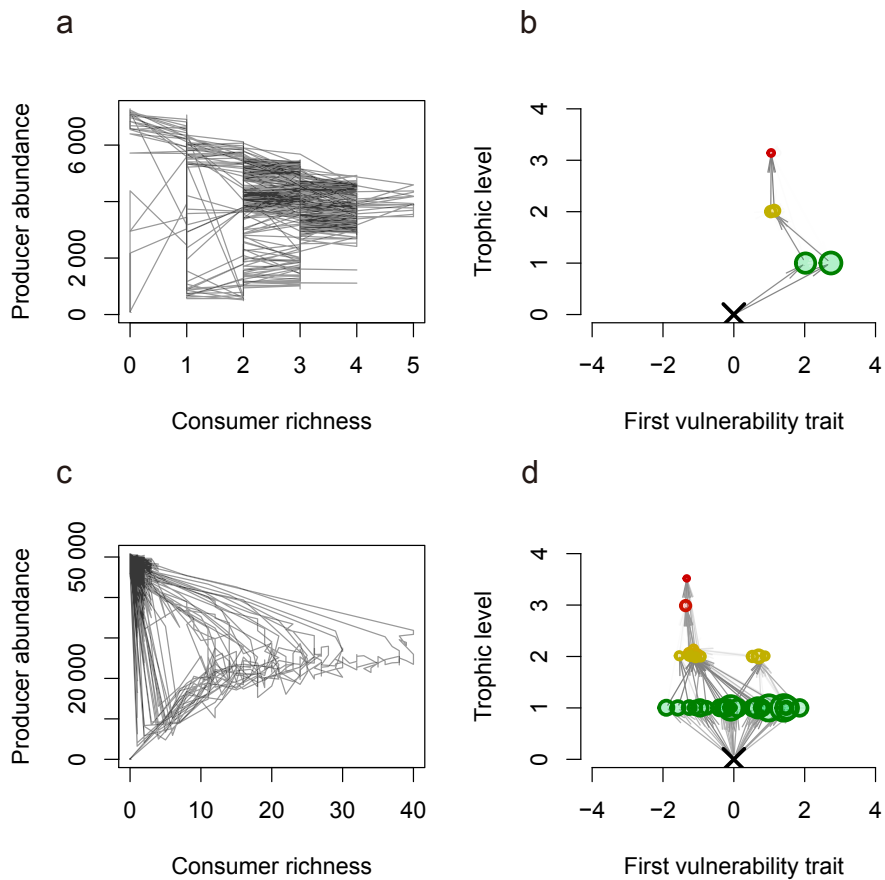
#### Robustness checks

As summarized in Section 3.4 of the main text, we test the effects of different choices of the cost minimum for vulnerability traits (Fig. S1), trait-space dimensionalities (one-dimensional and three-dimensional foraging and vulnerability trait vectors, Fig. S2), larger trophic efficiency ( $a=0.9$ ; Fig. S3), larger abundance of the external resource ( $N_R=9,000$ ; Fig. S4), and different combinations of the scales of foraging intensities ( $C_F=0.45$ ,  $0.9$ , and  $1.8$ ) and interference-competition intensities ( $C_I=0.05$ ,  $0.1$ ,

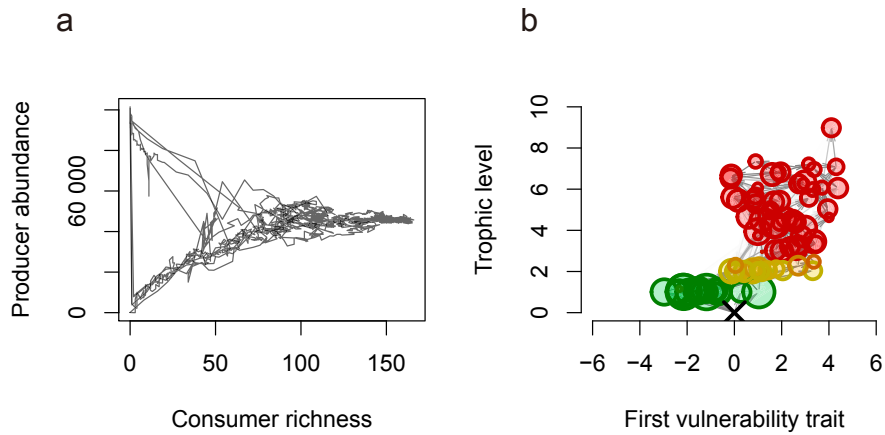
and  $0.2$ ; Fig. S5a,b). Furthermore, we relax the assumption of equal variances of the offspring trait distributions for foraging and vulnerability traits ( $\sigma_{m,f}=0.01$  and  $0.09$  with  $\sigma_{m,v}=0.03$ ; Fig. S6). Finally, we introduce handling times, leading to a Holling-type-II functional response instead of a linear functional response; based on this model extension, we investigate large and small handling times ( $h=1/8000$ , and  $1/800$ ; Fig. S7). As discussed in Section 3.4 of the main text, cyclic transitions are observed in nearly all resultant evolving communities.



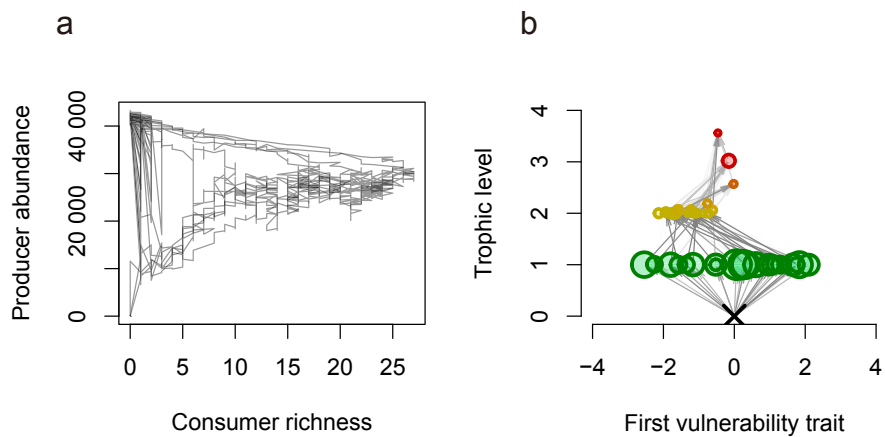
**Fig. S1.** Robustness with respect to altering the cost minimum for vulnerability traits. The choices (a) (1,0) and (b) (2.5,0), respectively, correspond to a moderate distance and a large distance of the cost minimum from the vulnerability trait vector of the external resource. For moderate differences, the result remains qualitatively unchanged (a), whereas larger differences make the re-emergence of the trophic structure difficult (b).



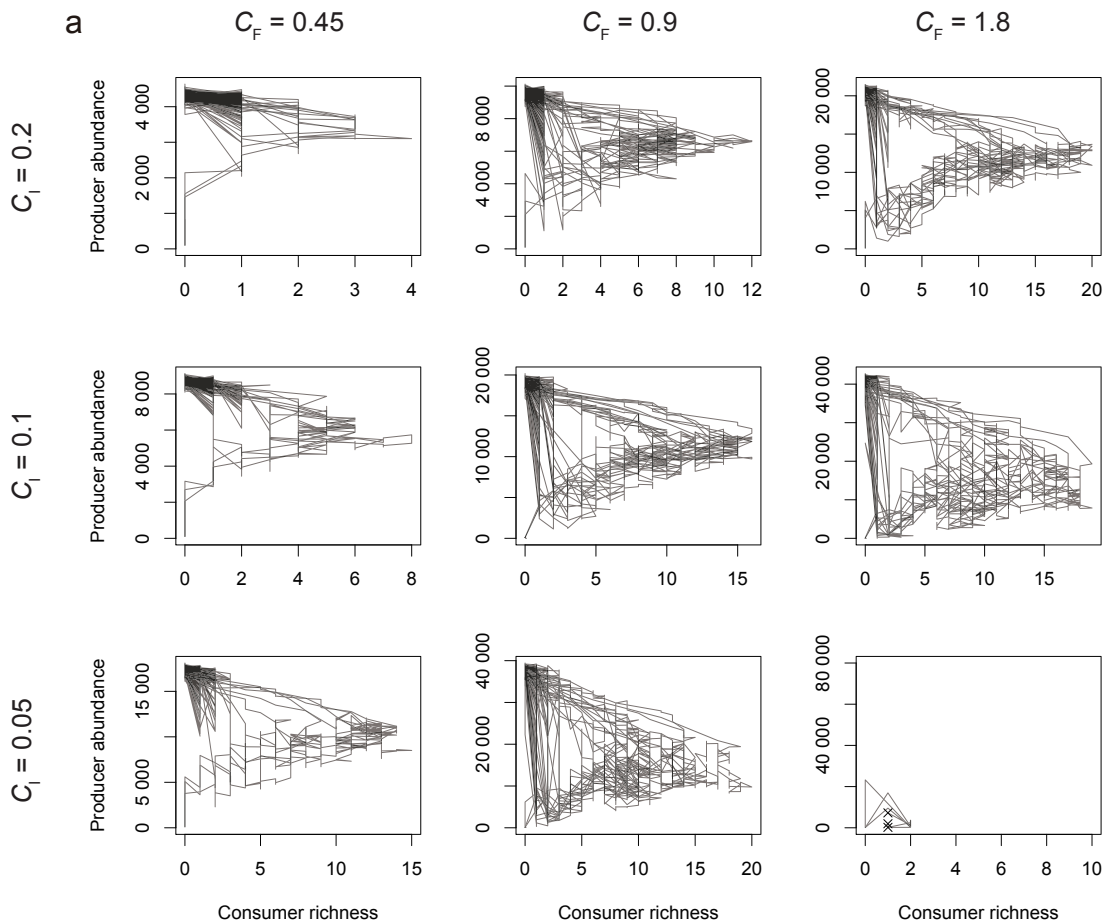
**Fig. S2.** Robustness with respect to altering the trait-space dimensionality. We show results for a one-dimensional trait space (a, b) and a three-dimensional trait space (c, d). (a, c) Curves show the time course of consumer richness and producer abundance. Each time course is obtained from three independent model runs. (b, d) Circles represent species, with their areas being proportional to the species' abundance, their colors indicating the species' trophic level, and their horizontal positions indicating the species' first vulnerability trait. The cross at trophic level 0 represents the external resource. Arrows indicate trophic links, with darker colors indicating stronger interactions. Cyclic transitions between the HTL state and the LTL state are observed both for a one-dimensional trait space (a, b) and for a three-dimensional trait space (c, d), with the relative duration of the LTL state increasing with the dimensionality. Snapshots of the corresponding HTL states show that species richness significantly increases with trait-space dimensionality (b, d).



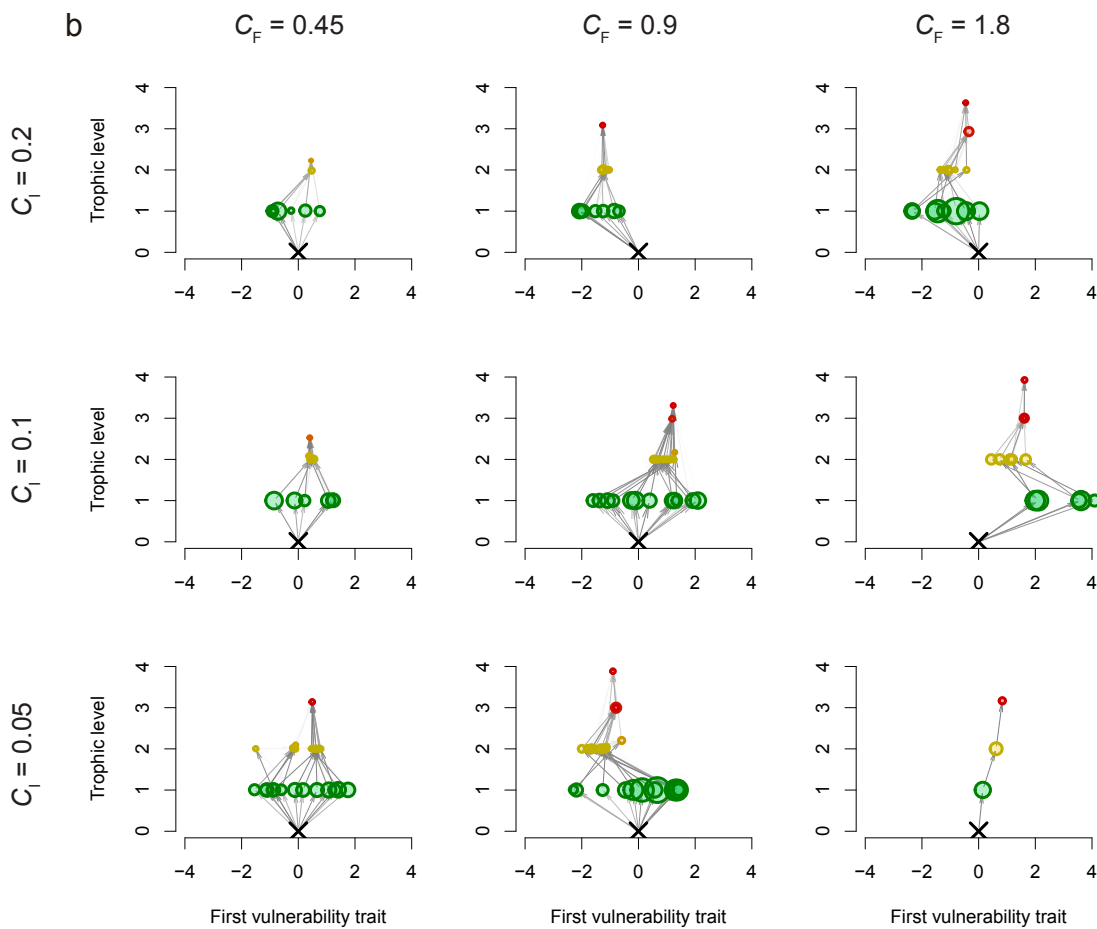
**Fig. S3.** Robustness with respect to increased trophic efficiency,  $a = 0.9$ . (a) The curve show the time course of consumer richness and producer abundance obtained from a single model run. (b) Circles represent species, with their areas being proportional to the species' abundance, their colors indicating the species' trophic level, and their horizontal positions indicating the species' first vulnerability trait. The cross at trophic level 0 represents the external resource. Arrows indicate trophic links, with darker colors indicating stronger interactions. The community's overall behavior remains the same, except for higher trophic levels and larger species richness.



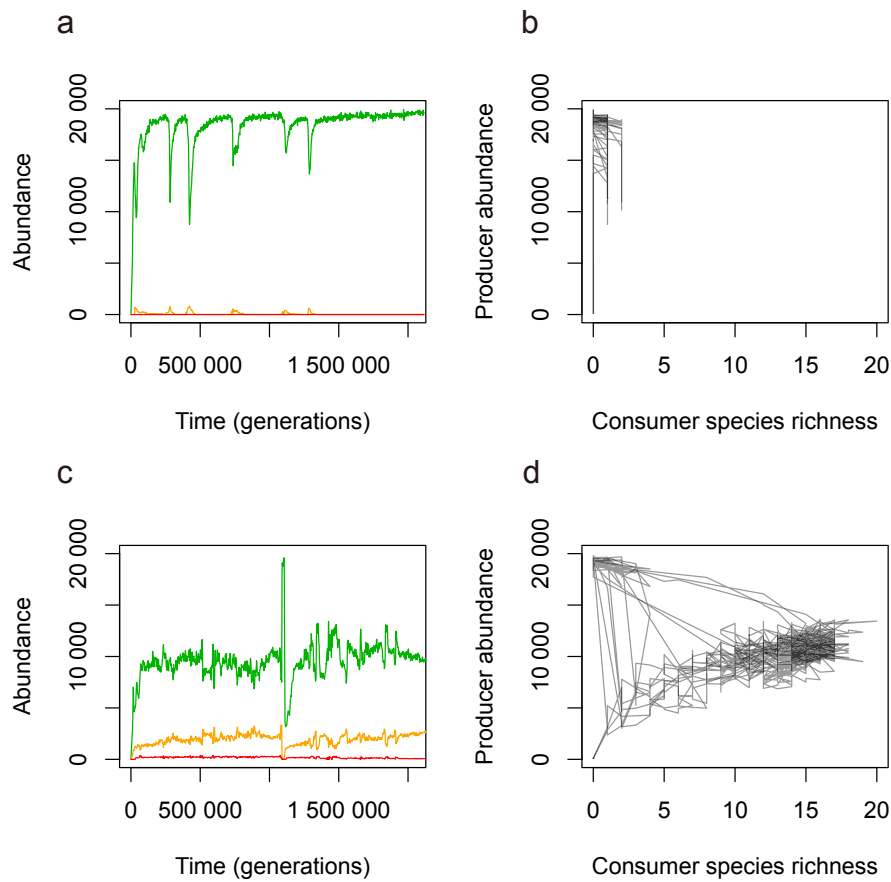
**Fig. S4.** Robustness with respect to increased abundance of the external resource,  $N_R = 9,000$ . (a) The curve shows the time course of consumer richness and producer abundance obtained from three independent model runs. (b) Circles represent species, with their areas being proportional to the species' abundance, their colors indicating the species' trophic level, and their horizontal positions indicating the species' first vulnerability trait. The cross at trophic level 0 represents the external resource. Arrows indicate trophic links, with darker color indicating stronger interactions. The community's overall behavior remains similar, except for a prolonged duration of the HTL state.



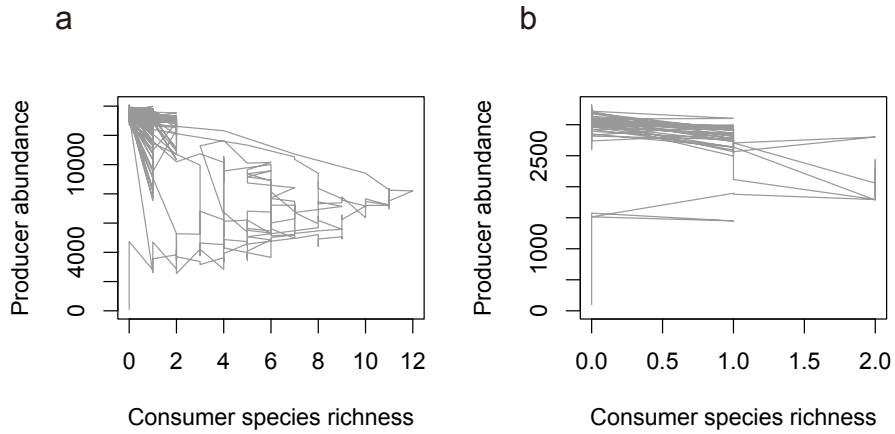
**Fig. S5a.** Robustness with respect to altering the scales of foraging intensities and interference-competition intensities: effect on cyclic dynamics. Curves show the time course of consumer richness and producer abundance obtained from three model runs. Consumers tend not to re-emerge when foraging intensities are low and interference competition is strong ( $C_F = 0.45$  and  $C_I = 0.1, 0.2$ ). Communities quickly become extinct (cross marks) when foraging intensities are high and interference competition is weak ( $C_F = 0.2$  and  $C_I = 0.05$ ). Otherwise, cyclic transitions between the HTL state and the LTL state are observed.



**Fig. S5b.** Robustness with respect to altering the scales of foraging intensity and interference-competition intensity: effect on community structure. Circles represent species, with their areas being proportional to the species' abundance, their colors indicating the species' trophic level, and their horizontal positions indicating the species' first vulnerability trait. The cross at trophic level 0 represents the external resource. Arrows indicate trophic links, with darker color indicating stronger interactions. The bottom-right panel shows a community just before its extinction (see also the corresponding panel in Fig. S5a). Low foraging intensities tend to reduce the maximum trophic level.



**Fig. S6.** Robustness with respect to altering the variances of the offspring trait-distributions for foraging and vulnerability traits. With  $\sigma_{m,v} = 0.03$ , we show results for (a, b)  $\sigma_{m,f} = 0.01$  and (c, d)  $\sigma_{m,f} = 0.09$ . (a, c) Curves show the time course of the abundances of producers (green), trophic-level-2 consumers (yellow), and higher-trophic-level consumers (red). (b, d) Curves show the time course of consumer richness and producer abundance. All curves are obtained from three independent model runs. Larger variances for foraging traits stabilize the HTL state and shorten the recovery time from the LTL state (c, d).



**Fig. S7.** Robustness with respect to introducing handling times, leading to a nonlinear functional response. We consider a Holling-type-II functional response with an attack rate of 1 and different handling times, (a)  $h = 1/8,000$  and (b)  $h = 1/800$ . Curves show the time course of consumer richness and producer abundance obtained from a single model run. If handling times are sufficiently small (a), we observe the same evolutionary cycles as with the linear response.